

*Data Reduction  
and Thermal Product Determination  
for Single and Two-layered Substrate  
Thin-film Gauge*

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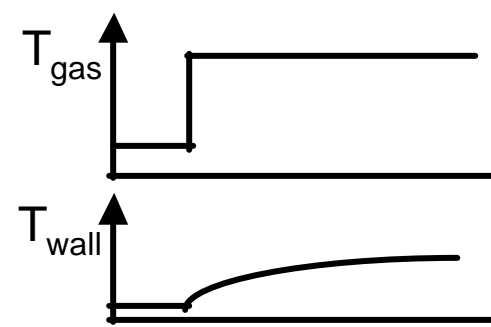
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1. **Thin film gauge operating principle**
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# Thin film gauge operating principle

Heat transfer coefficient

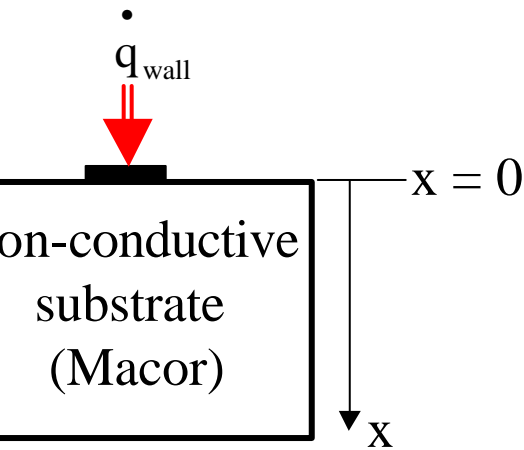
$$h = \frac{\dot{q}_{\text{wall}}(t)}{(T_{\text{gas}} - T_{\text{wall}}(t))}$$



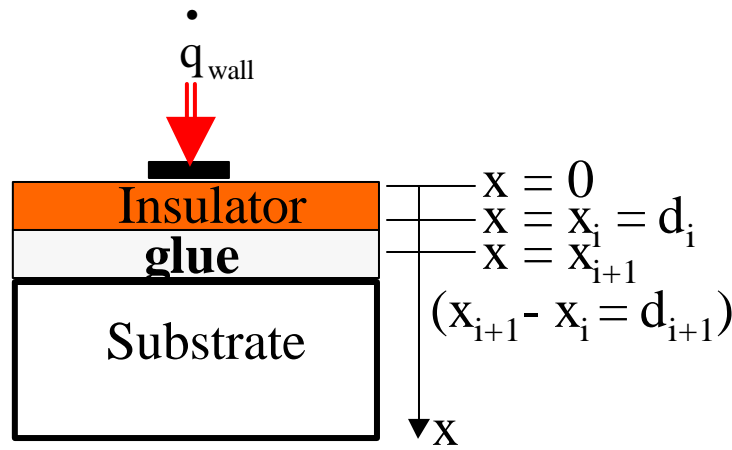
Unsteady conduction

$$\frac{\partial^2 T_i(x, t)}{\partial x^2} = \frac{1}{a_i} \frac{\partial T_i(x, t)}{\partial t}$$

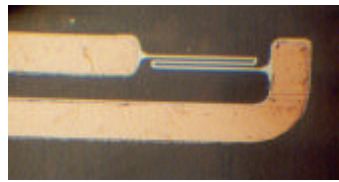
with  $a_i = \frac{k_i}{\rho_i C_i}$



Single-layer



Two-layer



❖ 1D conduction

❖ Semi-infinite subs

• Heat flux at the w

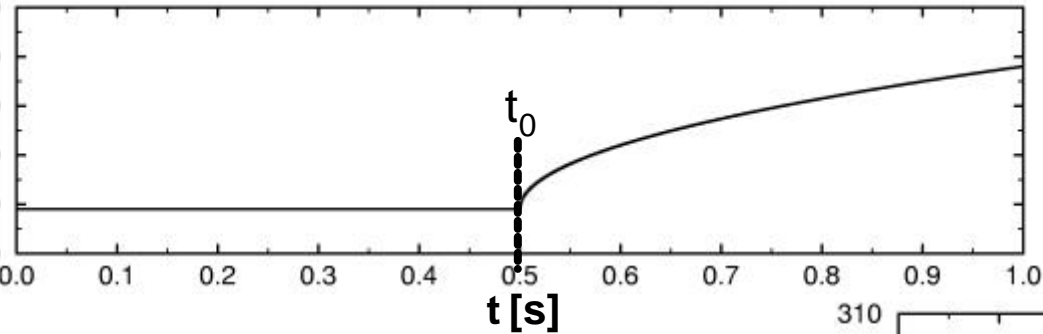
$$\dot{q}_{\text{wall}}(t) = -k_1 \left( \frac{\partial T_1}{\partial x} \right)_{x=0}$$

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# Analytical solution

## 2.1 Single-layer thin-film gauge

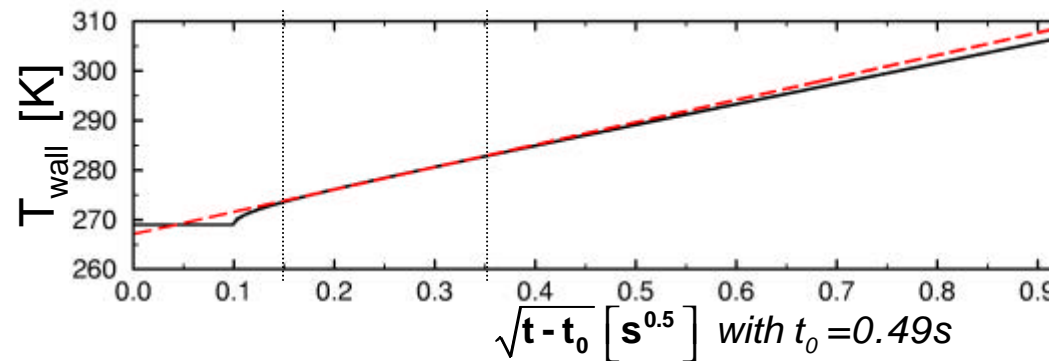
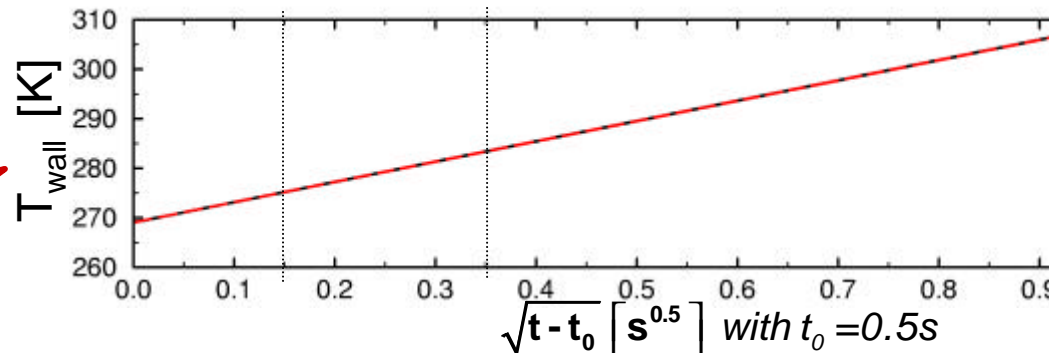


- Linear law in  $\sqrt{t}$

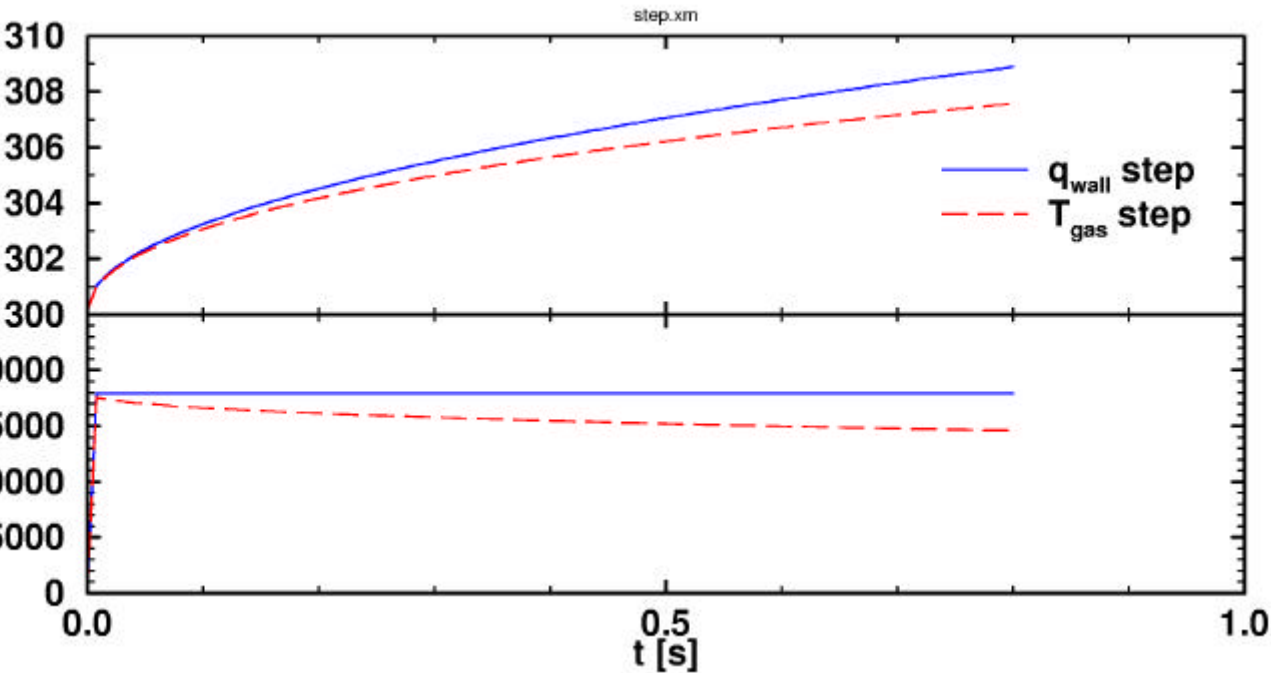
$$T_{\text{wall}}(t) - T_0 = \frac{2}{\sqrt{p}} \frac{\dot{q}_{\text{wall}}}{\sqrt{C k}} \sqrt{t}$$

Error induced by  $t_0$

0.01s of error in  $t_0$   
 >10% error on heat flux  
 ( $\dot{q}_{\text{wall}} = 75250 \text{ W/m}^2$ )



# Single-layer thin-film gauge



gas step  
solution

$$\frac{T_{\text{wall}}(t) - T_{\text{wall}}(t=0)}{T_{\text{gas}} - T_{\text{wall}}(t=0)} = 1 - e^{(\beta^2)} \text{erfc}(\beta)$$

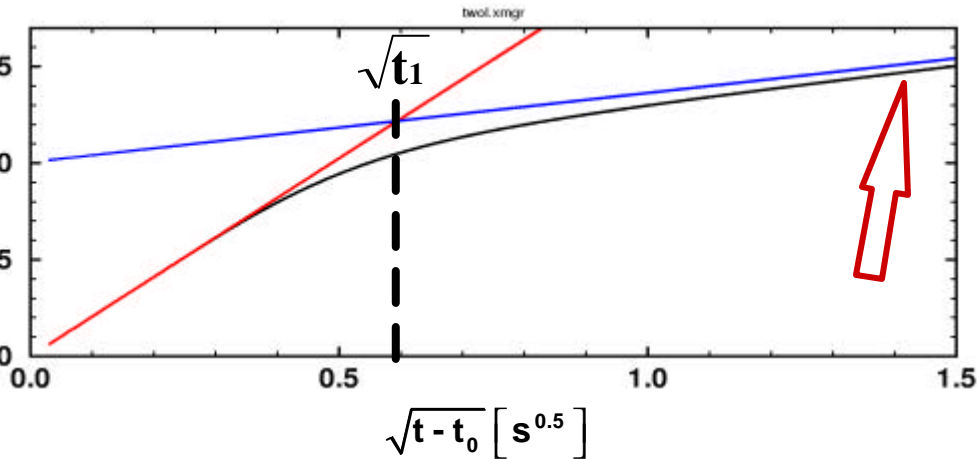


Depends only

$$\beta = \frac{h\sqrt{t}}{\sqrt{? C k}}$$

# Two-layer thin-film gauge

$$h_{II}(t) = \frac{2 \dot{q}_{\text{wall}}}{\sqrt{p} \sqrt{\rho_2 C_2 k_2}} \sqrt{t} + \dot{q}_{\text{wall}} \frac{d_1}{k_1} \left[ 1 - \frac{\rho_1 C_1 k_1}{\rho_2 C_2 k_2} \right]$$



- slopes  $\Rightarrow$  thermal properties
- "switch point"  $\Rightarrow$  thickness

$\Delta$  Error induced by  
finite temperature  
evolution

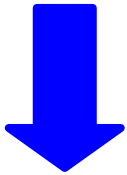
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# Numerical solution

Unsteady conduction equation solved thanks to finite difference Crank-Nicholson scheme :

$$\frac{\partial T(x, t)}{\partial t} = a \frac{\partial^2 T(x, t)}{\partial x^2}$$



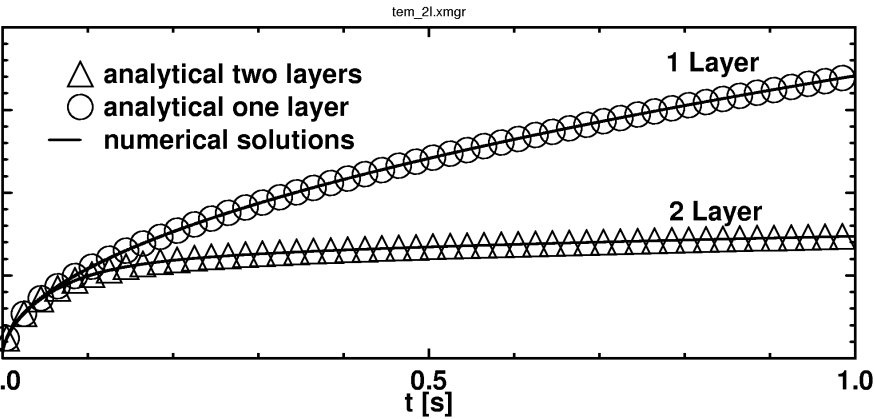
$$\frac{T_j^{m+1} - T_j^m}{\tau} = a \left[ \frac{\theta (T_{j-1}^{m+1} - 2 T_j^{m+1} + T_{j+1}^{m+1})}{\Delta x^2} + \frac{(1-\theta)(T_{j-1}^m - 2 T_j^m + T_{j+1}^m)}{\Delta x^2} \right]$$

If  $\theta > 0.5$ , the scheme is unconditionally stable  
 $\Rightarrow$  space step and time step are independent.

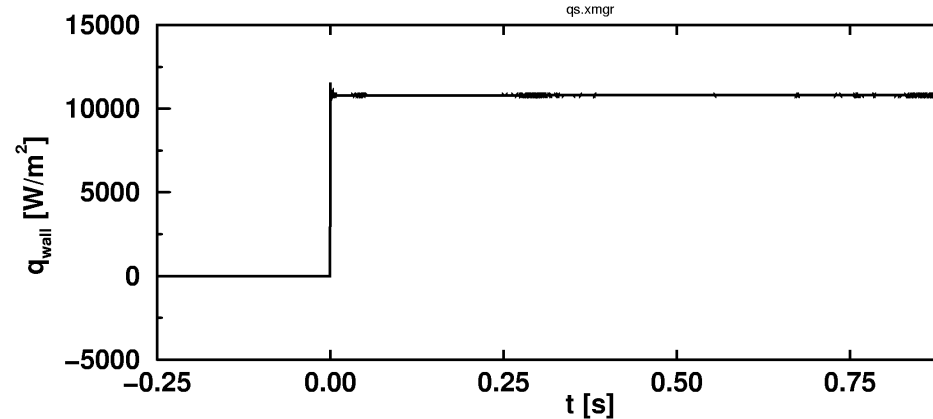
# Numerical solution

## Validation

surface temperature  $T_{\text{wall}}(t)$



surface heat flux  $q_{\text{wall}}(t)$



♣ Very flexible, no constraint

**ACCURATE**  $\dot{q}_{\text{wall}}$

$\hat{U}$

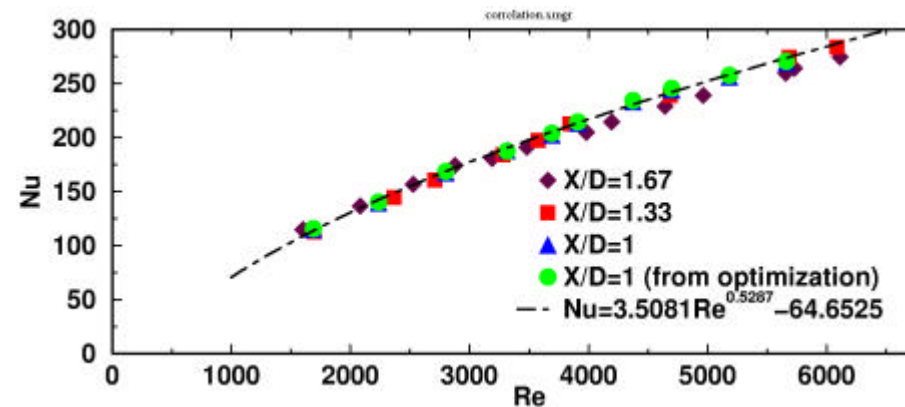
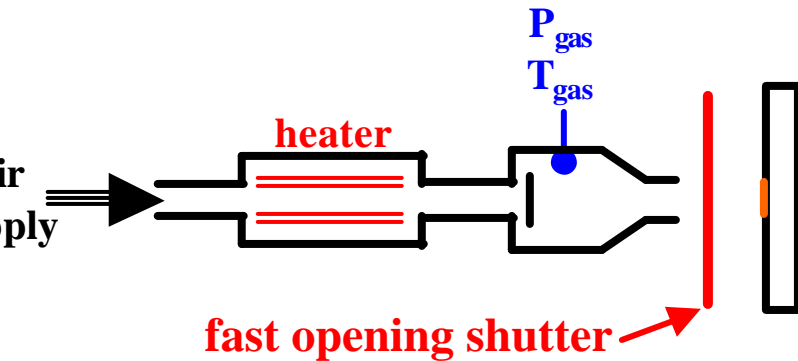
**ACCURATE**  $\sqrt{?_1 C_1 k_1}$  ,  $d_1$  **and**  $\sqrt{?_2 C_2 k_2}$  **(needed)**

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# Thermal properties determination

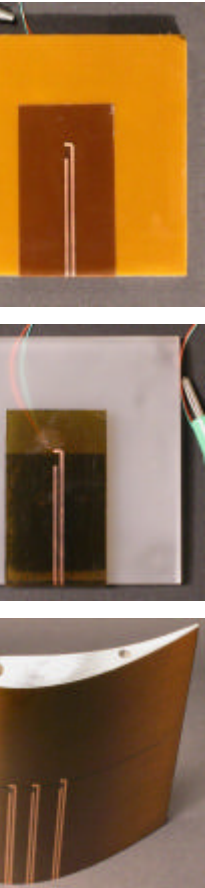
## 4.1 Heat flux source characterization using a reference gauge



- Various  $P_{\text{gas}}$  and  $T_{\text{gas}}$

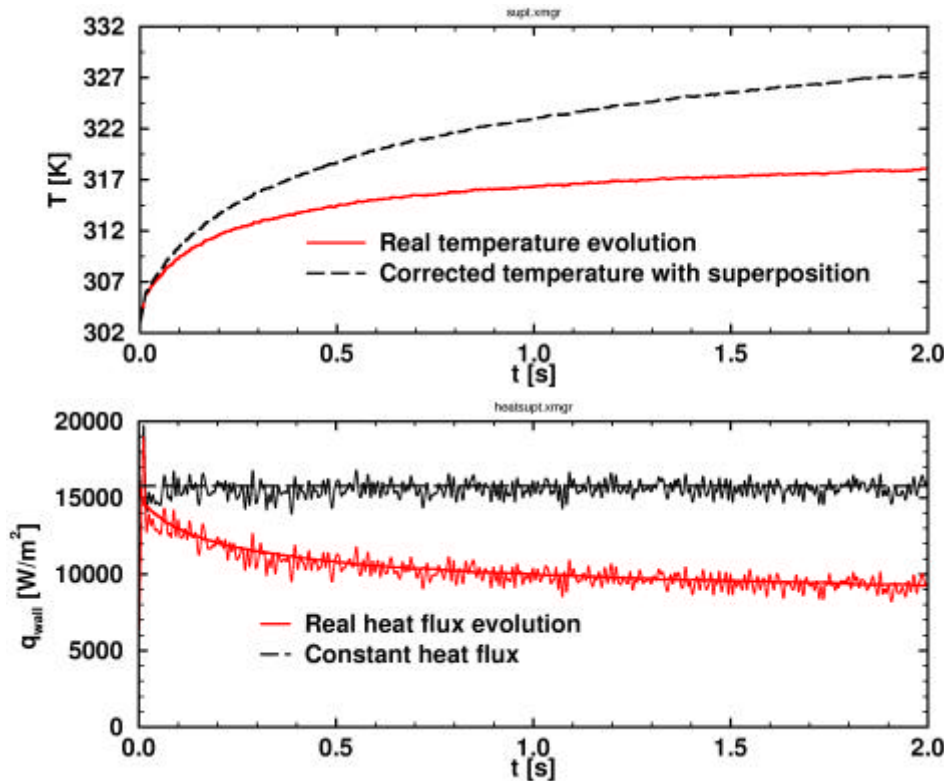
$\text{P correlation } Nu = 3.5081 Re^{0.5287} - 64.6525$

# 2 Calibration using analytical solution

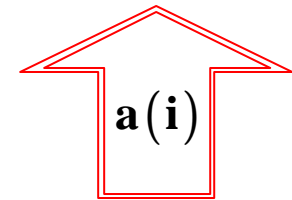


$\Delta$  Analytical solution valid for constant heat flux

Conditioning temperature evolution with superposition technique



$$T_{wall 2}(n) = \sum_{i=0}^n (a(i) T_{wall 1}(n-i))$$



$$\dot{q}_{wall 2}(n) = \sum_{i=0}^n (a(i) \dot{q}_{wall 1}(n-i))$$

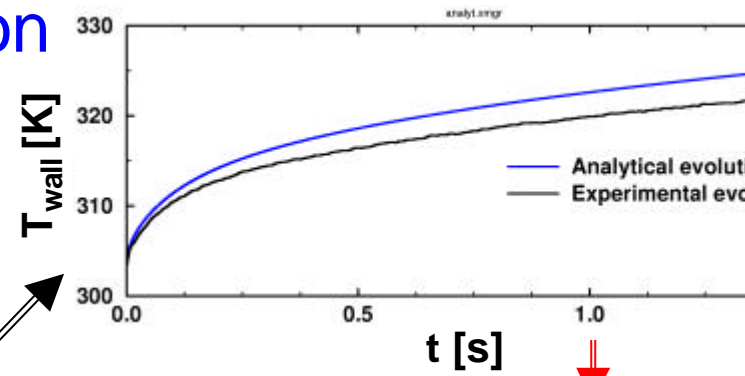
# 2 Calibration using analytical solution

$\dot{q}_{\text{wall}}$  from  $Nu = 3.5081 Re^{0.5287} - 64.6525$

Two-layer analytical solution

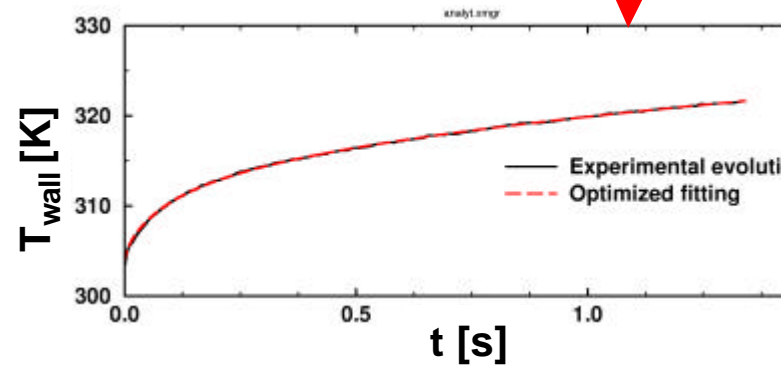
$$T_{\text{wall}}(t) = \frac{2 \dot{q}_{\text{wall}}}{\sqrt{p} \sqrt{?_2 C_2 k_2}} \sqrt{t} + \dot{q}_{\text{wall}} \frac{d_1}{k_1} \left[ 1 - \frac{?_1 C_1 k_1}{?_2 C_2 k_2} \right]$$

First guess  
 $\sqrt{?_i C_i k_i}, d_i$



$\sum (T_{\text{reconstructed}} - T_{\text{experiment}})$

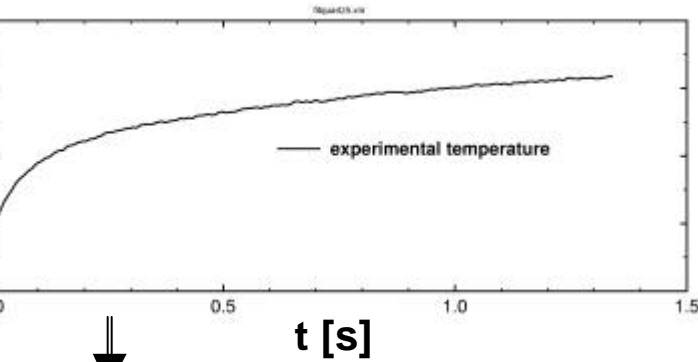
**Optimization routine**  
 new  $\sqrt{?_i C_i k_i}, d_i$



## 2 Calibration using analytical solution

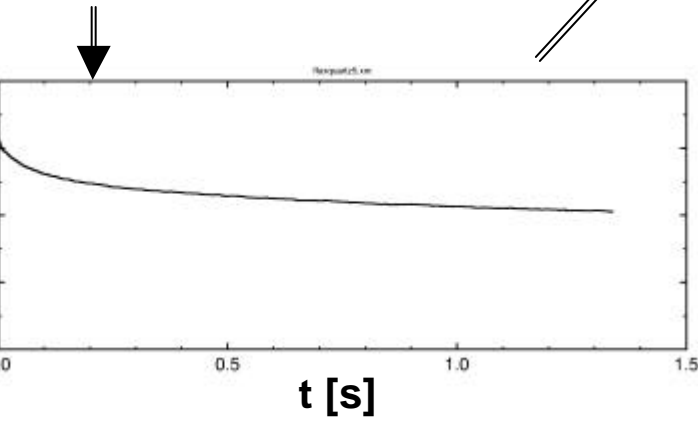
	$\sqrt{? C k}$ Upilex [J/m <sup>2</sup> Ks <sup>0.5</sup> ]	Upilex Thickness [μm]	$\sqrt{? C k}$ 2nd layer [J/m <sup>2</sup> Ks <sup>0.5</sup> ]
on Macor (8 tests)	<b>747</b>	<b>310</b>	<b>2255</b>
Dispersion (20:1)	2.1%	15.1%	6.1%
Standard value	<b>692</b>	<b>250 (350)</b>	<b>1780</b>
on quartz (9 tests)	<b>787</b>	<b>168</b>	<b>1763</b>
Dispersion (20:1)	3.7%	5.2%	5.1%
Standard value	<b>692</b>	<b>125 (150)</b>	<b>1521</b>
on steel (5 tests)	<b>732</b>	<b>177</b>	<b>10570</b>
Dispersion (20:1)	13.4%	10.2%	20.6%
Standard value	<b>692</b>	<b>125 (150)</b>	<b>8088</b>

# 3 Calibration using numerical solution



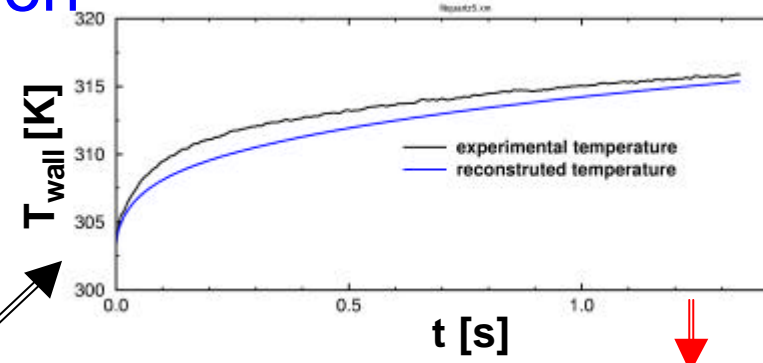
$$T_{\text{wall}}(t) = h (T_{\text{gas}} - T_{\text{wall}}(t))$$

$$Nu = 3.5081 Re^{0.5287} - 64.6525$$



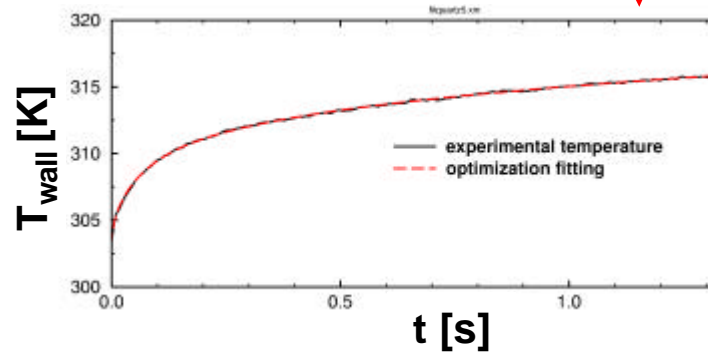
Crank-Nicholson

First guess  
 $\sqrt{?_i C_i k_i}, d_i$



$$\sum (T_{\text{reconstructed}} - T_{\text{experimental}})$$

**Optimization program**  
 new  $\sqrt{?_i C_i k_i}, d_i$



### 3 Calibration using numerical solution

	$\sqrt{? C k}$ Upilex [J/m <sup>2</sup> Ks <sup>0.5</sup> ]	Upilex Thickness [μm]	$\sqrt{? C k}$ 2nd layer [J/m <sup>2</sup> Ks <sup>0.5</sup> ]
on Macor (8 tests)	<b>731</b>	<b>305</b>	<b>2117</b>
Dispersion (20:1)	2.3%	3.9%	5.9%
Standard value	<b>692</b>	<b>250 (350)</b>	<b>1780</b>
on quartz (9 tests)	<b>752</b>	<b>167</b>	<b>1726</b>
Dispersion (20:1)	3.9%	3.9%	4.9%
Standard value	<b>692</b>	<b>125 (150)</b>	<b>1521</b>
on steel (5 tests)	<b>699</b>	<b>175</b>	<b>8147</b>
Dispersion (20:1)	8.8%	8.7%	9%
Standard value	<b>692</b>	<b>125 (150)</b>	<b>8088</b>

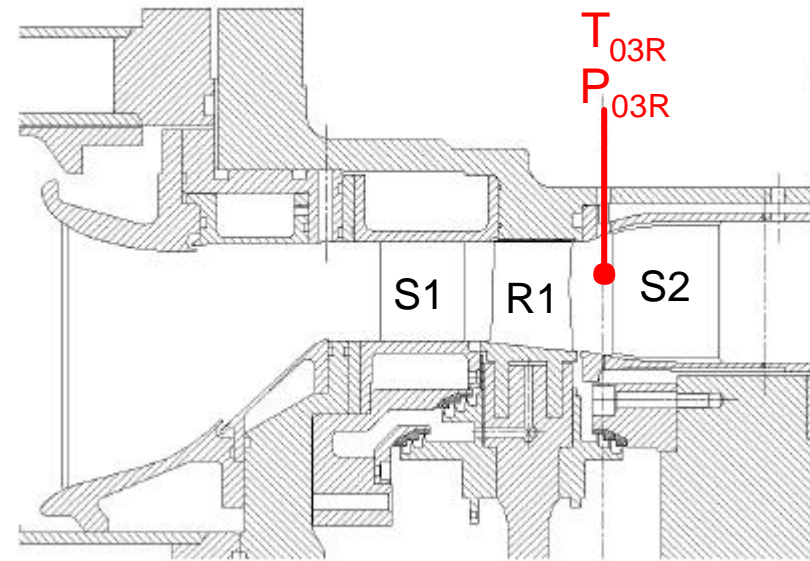
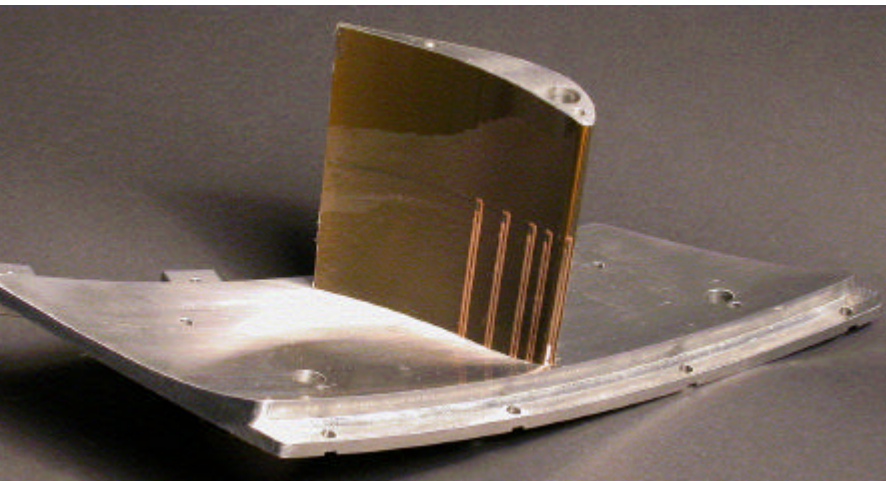
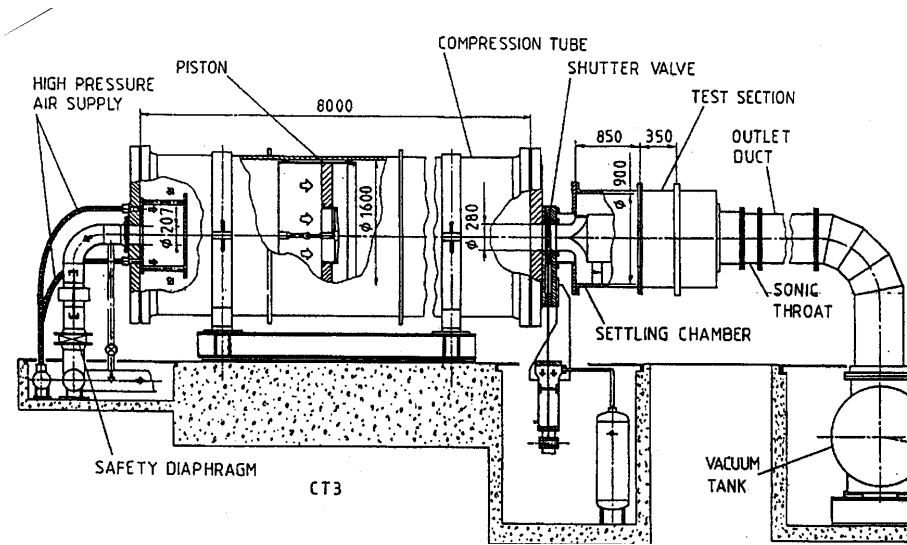
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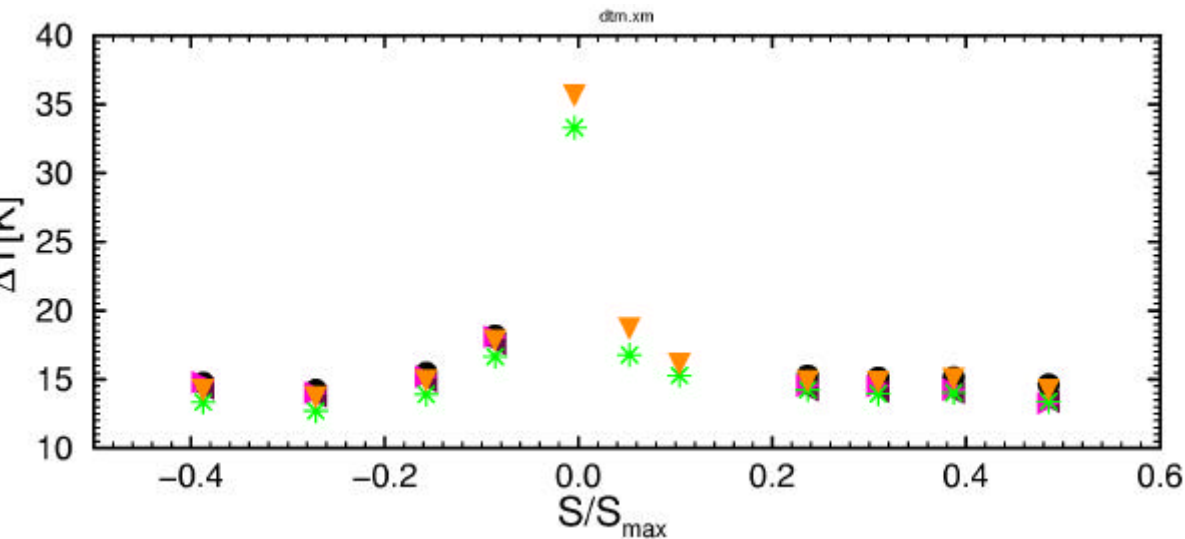
# Example of measurement

Blowdown wind tunnel,  
1.5 transonic stage

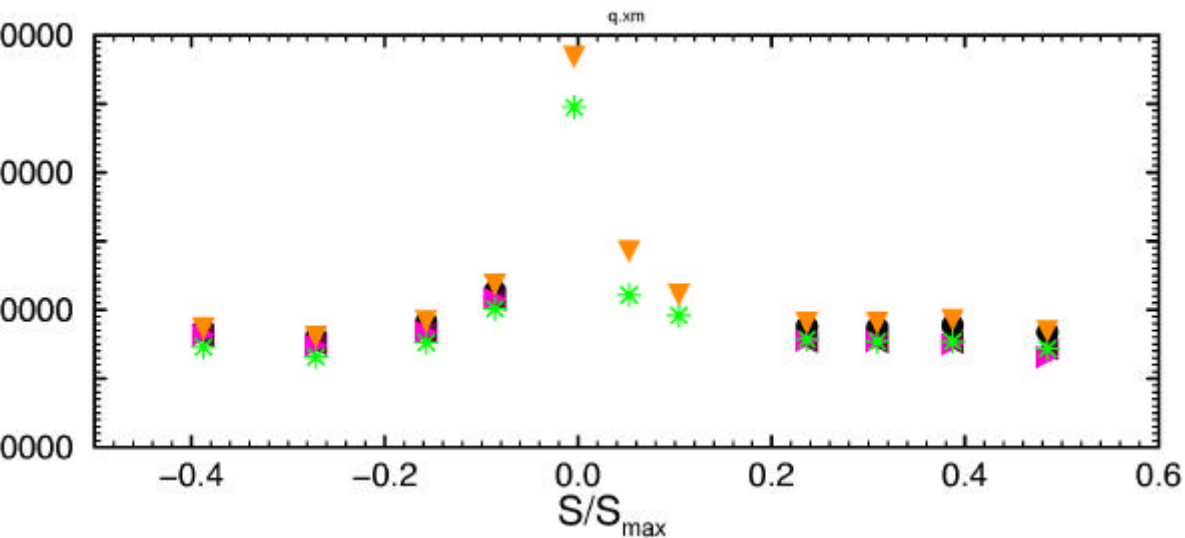
Design rotational speed:  
6500 RPM



# Time-averaged results

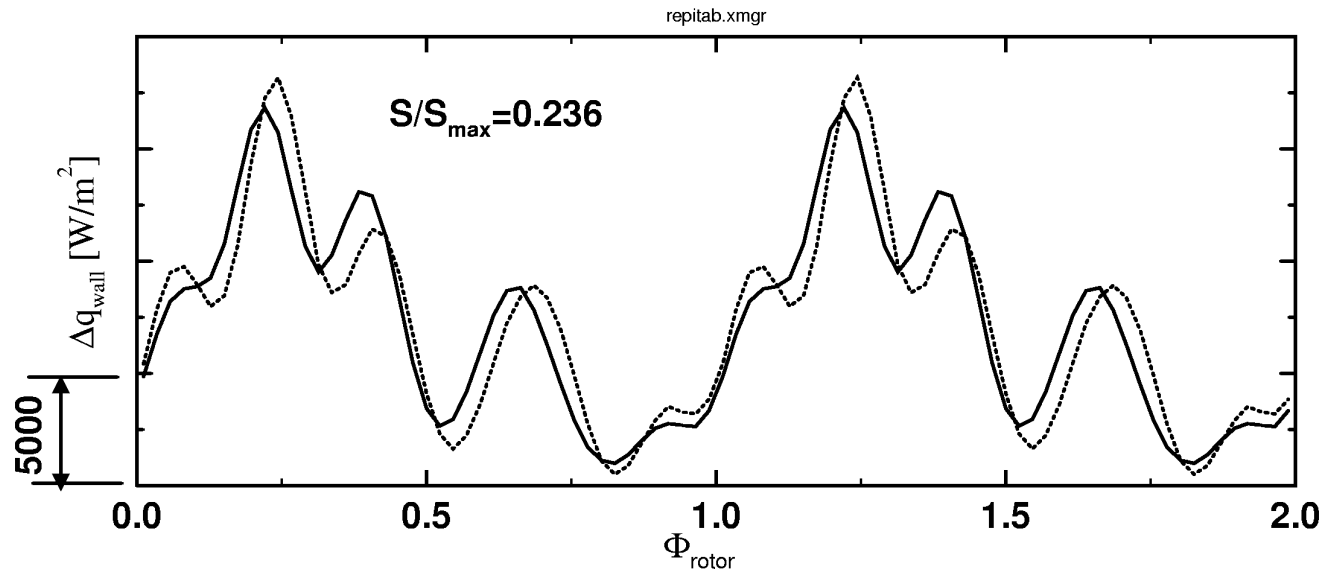


- Averaging around design rotational speed



- Computed with Cranley and Nicholson scheme

## 2 Time-resolved results



- Phase-locked average on 3 rotor revolutions

# Conclusions

Flexible heat flux computation with Crank-Nicholson scheme

Calibration of two-layer gauges:

1<sup>st</sup> method fits analytical solutions instead of linearizing

2<sup>nd</sup> method uses Crank-Nicholson scheme

and can be applied without restriction

Measurement on CT3:

successful use of the gauge

heat flux with Crank-Nicholson scheme

## Perspectives

Measurement on CT3:

comparison with ceramic inserts

⇒ validation of two-layer thin-film gauge

