SUPPORTING INFORMATION

Ultrafast Electronic Relaxation Dynamics of Atomically Thin MoS$_2$ is Accelerated by Wrinkling

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1. **Height and width profiles of multilayer MoS$_2$ wrinkles**

Fig. S1a is an AFM image of wrinkles in 17L-MoS$_2$. We select 3 wrinkles and take height profiles along 3 lines for each wrinkle (Fig. S1b).

![AFM image and height profiles](image)

**Figure S1.** (a) AFM image of wrinkled 17L-MoS$_2$. (b) Height profiles along line 1, 2, 3 (on wrinkle 1); 4, 5, 6 (on wrinkle 2); and 7, 8, 9 (on wrinkle 3). Colored lines are fits to Eq. S1.
All height profiles are fit to the function\(^1\):

\[
h(x) = \frac{\delta}{2} \left( 1 + \cos \frac{2\pi x}{\lambda} \right) + h_0,
\]

where \(\delta\) and \(\lambda\) are the height and width of the wrinkle, respectively, and \(h_0\) is the offset.

The fitting results are summarized in Table S1.

**Table S1.** Heights \(\delta\) and widths \(\lambda\) of lines 1 – 9 of wrinkles 1 – 3. The errors correspond to the standard deviation.

<table>
<thead>
<tr>
<th>Line</th>
<th>Line 1</th>
<th>Line 2</th>
<th>Line 3</th>
<th>Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Wrinkle 1</strong></td>
<td><strong>Height (\delta) ((\mu)m)</strong></td>
<td>0.50</td>
<td>0.50</td>
<td>0.50</td>
</tr>
<tr>
<td></td>
<td><strong>Width (\lambda) ((\mu)m)</strong></td>
<td>2.05</td>
<td>2.08</td>
<td>2.08</td>
</tr>
<tr>
<td><strong>Wrinkle 2</strong></td>
<td><strong>Height (\delta) ((\mu)m)</strong></td>
<td>0.34</td>
<td>0.34</td>
<td>0.33</td>
</tr>
<tr>
<td></td>
<td><strong>Width (\lambda) ((\mu)m)</strong></td>
<td>1.75</td>
<td>1.80</td>
<td>1.79</td>
</tr>
<tr>
<td><strong>Wrinkle 3</strong></td>
<td><strong>Height (\delta) ((\mu)m)</strong></td>
<td>0.29</td>
<td>0.30</td>
<td>0.31</td>
</tr>
<tr>
<td></td>
<td><strong>Width (\lambda) ((\mu)m)</strong></td>
<td>1.78</td>
<td>1.74</td>
<td>1.82</td>
</tr>
</tbody>
</table>

### 2. Static PEEM image

The static PEEM image obtained with 3.61-eV illumination is shown in Fig. S2a. The image contrast between flat (bright) and wrinkled (dark) portions of 17L-MoS\(_2\) is opposite to that expected based on topography.\(^2\) This could be attributed to the calculated VB DOS being lower for wrinkled than for flat MoS\(_2\) (see Fig, S2b). Thus, the photoionization cross-section is smaller for wrinkled MoS\(_2\).
3. Determination of photon order and probe window

We perform fluence dependence measurements to determine the photon order of the 2.41-eV pump and 3.61-eV probe pulse interactions with wrinkled 17L-MoS₂. The photoemission intensity is given as\(^3,4\):

\[
S = \sigma_{pu} \cdot F_{pu}^N \cdot \sigma_{pr} \cdot F_{pr}^N,
\]

where \(S\) is total photoemission signal, \(\sigma_{pu}\) (\(\sigma_{pr}\)) is the pump absorption (probe ionization) cross-section, \(F_{pu}\) (\(F_{pr}\)) is the fluence of the pump (probe) pulse, and \(N_{pu}\) \((N_{pr})\) is the pump (probe) photon order. Figs. S3a,b show that the PEEM signal scales linearly with pump and probe fluence, respectively. Hence, both pump and probe pulses each interact with the 17L-
MoS$_2$ sample via a one-photon process.

The probe photon order is used to establish the probe window (Fig. S4). In photoemission, the probe window arises from the requirement to conserve in-plane momentum$^5$, and defines the region of the band structure from which e can be ejected.$^5$ The band structure from Ref. 6 is for b-MoS$_2$ in vacuum, calculated within the $G_0W_0$ approximation.

To enable comparison with our experiments, we shift the lowest-energy CB to reproduce the experimental $K_v$–$K_e$ band gap of 1.95eV.$^7$ We also use the experimental ionization energy~5.47eV$^8$ for b-MoS$_2$ to determine the photoemission probe window.

4. **Extended time traces of the wrinkled and flat regions of multilayer MoS$_2$**

Fig. 4c shows the time traces of wrinkled and flat regions of the 17L-MoS$_2$ sample over a time delay range of 0 – 0.5 ps so that their different decay dynamics can be clearly seen. Here, we show the time traces over an extended range of –0.5 – 1.5ps. Those of wrinkled (Fig. S5a) and flat 17L-MoS$_2$ (Fig. S5b) are fit to one single exponential decay at positive time delay and

![Figure S4. Band structure (from Ref. 6) of bulk MoS$_2$, with one-photon 2.41-eV pump (green arrow) and one-photon 3.61-eV probe window (shaded regions).](image-url)
another at negative time delay, both convolved with the instrumental response function. At
negative time delay, the 3.61-eV pulse serves as the photoexcitation pump pulse, whereas the
2.41-eV pulse serves as the photoionization probe pulse, reversing the roles of these two pulses
at positive time delays. The decay observed at negative time delays therefore arises from
dynamics induced by 3.61-eV excitation.

5. Distributions of time constants for other wrinkles

The histogram of lifetimes for wrinkle 1 is in Fig. 5b. From the lifetime map (Fig.S6a), we

![Figure S5. Extended TR-PEEM time traces of (a) wrinkled and (b) flat 17L-MoS₂.](image)

![Figure S6. (a) Lifetime map of the electronic relaxation dynamics of 17L-MoS₂. (b) Histograms of time constants for wrinkles 2 (top panel) and 3 (bottom panel).](image)
extract the distributions of time constants for the other two wrinkles (Fig. S6b). For wrinkles 2 and 3, these are characterized by mean values (standard deviations) of 84 fs (13 fs) and 91 fs (14 fs), respectively. Both wrinkles undergo faster electronic relaxation than the flat region, consistent with the result obtained for wrinkle 1.

6. Electronic structure of a larger wrinkled MoS$_2$ model

Two additional periodic systems, 50% larger than the models in the main text (Figs. 6a,b), are examined to validate the impact of wrinkles on electronic structure. Flat and curved B-MoS$_2$ are represented with rectangular simulations cells comprising $1 \times 15 \times 1$ unit cells (Figs. S7a,b). The flat B-MoS$_2$ (System C) extends along the armchair direction with 81.7 Å length (Fig. S7a). The same method to create the wrinkled system in the main text is used to build one with a wave shape (System D, Fig. S7b). This has a 50 Å radius of curvature along the armchair direction, and its length is reduced to 79.4 Å with the thickness increased to 6.54 Å for each monolayer. The curvature of the B-MoS$_2$ model system D is twice smaller than Fig. 6b.

The geometry optimization is performed with VASP$^{9-11}$ in the same way as described in the main text, employing the PBE exchange–correlation functional$^{12}$, the PAW method$^{13}$.

![Figure S7](image-url) Side views of optimized (a) flat and (b) curved B-MoS$_2$. System D is curved along the armchair direction of B-MoS$_2$. The box shows the supercell boundary in the calculation. (c) Electronic DOS for C and D, aligned to the CB edge.
and the DFT-D3 van der Waals correction.\textsuperscript{14,15} The Brillouin zone is sampled with $7\times1\times3$ \Gamma-centered Monkhorst-Pack grids, the energy cutoff for the plane wave basis is set to 340 eV, and the convergence criterion of geometry optimization on atomic forces is 0.001 eV/Å. After geometry optimization, the radius of curvature for the wrinkled b-MoS\textsubscript{2} increases to 58 Å. Using the optimized structures, we compute the electronic DOS. The Brillouin zone sampling is increased to use $17\times1\times5$ \Gamma-centered Monkhorst-Pack grids. Fig. S6c indicates that the DOS of the curved system D rises faster from the CB edge, similar to the DOS observed for the smaller models in the main text (Fig. 6c). Because the NA coupling is inversely proportional to the energy gap, Eq. 2, it is larger in regions of higher DOS. The nonradiative e-ph relaxation is faster when DOS is higher.\textsuperscript{16,17} Therefore, the conclusions from the NAMD simulation with the smaller b-MoS\textsubscript{2} model hold for the larger one as well.

References


