

2 μ m Solid-State Laser Mode-locked By Single-Layer Graphene

A. A. Lagatsky¹, Z. Sun², T. S. Kulmala², R. S. Sundaram², S. Milana², F. Torrisi², O. L. Antipov³
Y. Lee⁴, J. H. Ahn⁴, C. T. A. Brown¹, W. Sibbett¹ and A.C. Ferrari^{2a)}

¹*School of Physics and Astronomy, University of St Andrews, St Andrews, KY16 9SS UK*

²*Department of Engineering, University of Cambridge, Cambridge CB3 0FA, UK*

³*Institute of Applied Physics, Russian Academy of Sciences, Nizhny Novgorod Russia*

⁴*School of Advanced Materials Science and Engineering and Advanced Institute of Nanotechnology, Sungkyunkwan University, Suwon 440-746, Korea*

We report a 2 μ m ultrafast solid-state Tm:Lu₂O₃ laser, mode-locked by single-layer graphene, generating transform-limited \sim 410fs pulses, with a spectral width \sim 11.1nm at 2067nm. The maximum average output power is 270mW, at a pulse repetition frequency of 110MHz. This is a convenient high-power transform-limited laser at 2 μ m for various applications, such as laser surgery and material processing.

Ultrafast lasers operating at \sim 2 μ m are of great interest due to their potential in various applications, e.g. telecoms¹, medicine^{2,3}, material processing^{3,4} and environment monitoring⁵. They can be used for light detection and ranging measurements⁵ and free-space optical communications⁵, due to the 2-2.5 μ m atmospheric transparency window⁵. Because water (main constituent of human tissue) absorbs more strongly at \sim 2 μ m (\sim 100/cm)³ than at other conventional laser wavelengths (e.g. \sim 10/cm at \sim 1.5 μ m, and \sim 1/cm at \sim 1 μ m)³, sources working at \sim 2 μ m are promising for medical diagnostic³ and laser surgery³. Currently, the dominant technique for ultrafast pulse generation at 2 μ m relies on semiconductor saturable absorber mirrors (SESAMs)^{6,7}. In-GaAsSb quantum-well-based SESAMs have been used to mode-lock Tm:Ho:NaY(WO₄)₂⁸ and Tm:Sc₂O₃⁹ lasers, generating 258fs pulses with 155mW output power at 2 μ m⁸, and 246fs pulses with 325mW output at 2.1 μ m⁹. However, SESAMs require complex growth techniques (e.g. molecular beam epitaxy⁶), often combined with ion implantation^{8,9} to reduce recovery time^{6,7}.

Nanotubes and graphene have emerged as promising saturable absorbers (SA), due to their low saturation intensity¹⁰⁻¹⁴, low-cost¹⁰ and easy fabrication^{12,14,15}. With nanotubes, broadband operation can be achieved by using a distribution of tube diameters^{10,16}. With graphene, this is intrinsic, due to the gapless linear dispersion of Dirac electrons^{12,14}. Ultrafast pulse generation at 0.8¹⁷, 1¹⁸, 1.3¹⁹ and 1.5 μ m^{10-12,14,20-23} was demonstrated with graphene-based SAs (GSAs). Ref.25 reported a 1.94 μ m Tm-doped fiber laser mode-locked by a polymer composite with graphene produced by liquid phase exfoliation of graphite^{14,24}. Compared to solid-state lasers, fiber lasers have some advantages, such as compact geometry and alignment-free operation. However, their output power is typically very low (\sim mW²⁶) and their output spectrum generally has side-bands²⁶. Solid-state lasers have the advantage, compared to fibre lasers, of sustaining ultrafast pulses with higher output power (typically \geq 100mW)^{6,7} and better pulse quality (e.g. transform-limited with sideband-free profile in

the spectral domain^{6,7}). Therefore, solid-state lasers are of interest for applications requiring high power and good pulse quality, such as industrial material processing⁶ and laser surgery³. Ref.27 used graphene-oxide to mode-lock a 2 μ m solid-state Tm:YAlO₃ laser. However, the output pulse duration was long, \sim 10ps, due to the lack of intracavity dispersion compensation²⁷. Also, graphene oxide^{29,30} is fundamentally different from graphene: it is insulating, with a mixture of sp²/sp³ regions^{29,30}, with many defects and gap states³⁰. Thus it may not offer the same wideband tunability as graphene. A mixture of 1 or 2 graphene layers grown by Chemical Vapor Deposition (CVD) was used to mode-lock a Tm-doped calcium lithium niobium gallium garnet (Tm:CLNGG) laser at 2 μ m in Ref.28. However, compared to 2 μ m solid-state lasers mode-locked by SESAMs^{8,9}, the output power was low (\sim 60mW), limited by damage to the mode-locker.

Here we report a single-layer graphene (SLG) mode-locked solid-state Tm:Lu₂O₃ laser at \sim 2067nm, with a 270mW average output power. Transform-limited \sim 410fs pulses are generated using a dispersion-compensated cavity. This is a convenient high-power transform-limited laser at 2 μ m for various applications.

Our GSA is prepared as follows. SLG is grown by CVD^{31,32}. A \sim 35 μ m thick Cu foil is heated to 1000 °C in a quartz tube, with 10sccm H₂ flow at \sim 5 \times 10⁻² torr. The H₂ flow is maintained for 30mins. This not only reduces the oxidized foil surface, but also extends the graphene grain size. The precursor gas, a H₂:CH₄ mixture with flow ratio 10:15, is injected at a pressure of 4.5 \times 10⁻¹ torr for 30mins. The carbon atoms are then adsorbed onto the Cu surface and nucleate SLG via grain propagation^{31,32}. The quality and number of layers are investigated by Raman spectroscopy^{33,34}, Fig.1. At the more common 514nm excitation, the Raman spectrum of CVD graphene on Cu does not show a flat background, due to Cu photoluminescence³⁵. This can be suppressed at 457nm, Fig.1. The spectrum does not show a D peak, indicating the absence of structural defects^{33,34,36}. The 2D peak is a single sharp Lorentzian, signature of SLG³³.

We then transfer a 10 \times 10mm² SLG region onto a quartz substrate (3mm thick) as follows. Poly(methyl methacrylate) (PMMA) is spin-coated on the sample. Cu is then dissolved in a 3% H₂O₂:35% HCl (3:1 ratio) mix-

^{a)}Electronic mail: acf26@eng.cam.ac.uk

ture, further diluted in equal volume of deionized water. The PMMA/graphene/Cu foil is then left floating until all Cu is dissolved. The remaining PMMA/graphene film is cleaned by moving it to a deionized H₂O bath, a 0.5M HCl bath, and again to a deionized H₂O bath. Finally, the layer is picked up using the target quartz substrate and left to dry under ambient conditions. After drying, the sample is heated to 180°C for 20mins to flatten out any wrinkles³⁷. The PMMA is then dissolved in acetone, leaving SLG on quartz. This is then inspected by optical microscopy, Raman spectroscopy and absorption microscopy. A representative Raman spectrum of the transferred sample is in Fig.1. After transfer, the 2D peak is still a single sharp Lorentzian, validating that SLG has indeed been transferred. The absence of a D peak proves that no structural defects are induced during this process^{33,34,36}. In order to estimate the doping, an analysis of more than 15 measurements with 514nm excitation is carried out. This wavelength is used since most previous literature and correlations were derived at 514nm³⁹. We find that the G peak position, Pos(G), up-shifts $\sim 4\text{cm}^{-1}$ in average after transfer on quartz, whereas the full width at half maximum of the G peak, FWHM(G), decreases from ~ 17 to $\sim 10.5\text{cm}^{-1}$. Also, the 2D to G intensity and area ratios, $I(2D)/I(G)$; $A(2D)/A(G)$, decrease from 3.2 to 1.6 and 5.8 to 5.3, respectively. This implies an increased p-doping compared to graphene on Cu before transfer³⁹⁻⁴¹. We estimate the doping for the sample on quartz to be $\sim 10^{13}\text{cm}^{-2}$, corresponding to a Fermi level shift $\sim 300/400\text{meV}$. For comparison, we also transferred on SiO₂/Si. In this case, the average Pos(G) and FWHM(G) are 1584cm^{-1} and 14cm^{-1} , respectively. The average Pos(2D) is 2685cm^{-1} , and $I(2D)/I(G)$; $A(2D)/A(G)$ are 3.2 and 7.1, respectively. This indicates a much lower doping, below 100meV. Therefore, we conclude that the doping of our graphene transferred on quartz does not arise from the transfer process itself, but it is most likely due to charge transfer from adsorbates on the substrate^{42,43}. The transmittance of the transferred SLG on quartz is then measured (Fig.2). The band at $\sim 270\text{nm}$ is a signature of the van Hove singularity in the graphene density of states⁴⁴, while those at $\sim 1.4, 2.2\mu\text{m}$ are due to quartz⁴⁵. The transmittance in the visible range (e.g. at $\sim 700\text{nm}$) is $\sim 97.7\%$ (i.e., $\sim 2.3\%$ absorbance), further confirming that the sample is indeed SLG⁴⁶. The absorbance decreases to $\sim 1\%$ at 2067nm, much lower than the 2.3% expected for intrinsic SLG. We assign this to doping⁴⁷. The graphene optical conductivity σ at a wavelength λ is: $\sigma(\lambda, E_F, T) = \frac{\pi e^2}{4h} [\tanh(\frac{\hbar c}{4k_B T} + \frac{2E_F}{\hbar c}) + \tanh(\frac{\hbar c}{4k_B T} - \frac{2E_F}{\hbar c})]$, as for Ref.47, where T is the temperature, E_F the Fermi energy. The transmittance (Tr) is linked to σ as:⁴⁷ $Tr \approx 1 - \frac{4\pi\sigma}{c}$. By fitting to the measured Tr we derive $E_F \sim 350\text{meV}$, consistent with the Raman estimates.

The laser setup is shown in Fig.3. The cavity consists of four plano-concave high-reflectivity ($R > 99.2\%$ at $2\mu\text{m}$) mirrors (M1-M4) and an output coupler (OC) with 1% transmittance at $2\mu\text{m}$, and is designed to ensure the

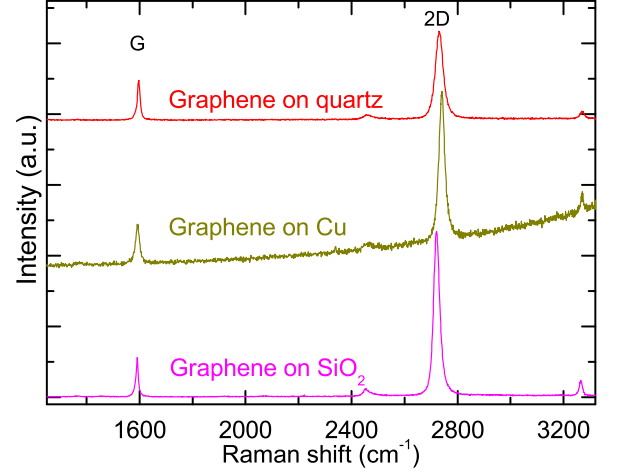


FIG. 1. Raman spectra at 457nm for graphene on Cu (before transfer) and after transfer on quartz and SiO₂/Si

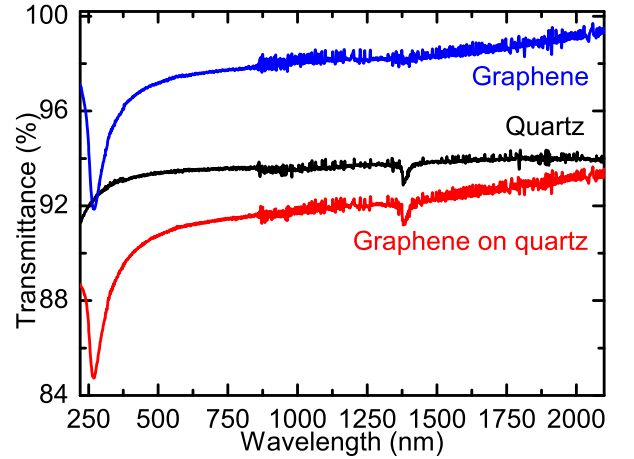


FIG. 2. Transmittance of quartz and graphene on quartz. For graphene, this is derived from the transmittance of transferred graphene on quartz divided by that of quartz.

best mode-matching between the pump and intra-cavity laser beams. Tm:Lu₂O₃ ceramic is selected as the gain material because of its high conductivity⁴⁸, broad emission spectrum ($>1.9\text{-}2.1\mu\text{m}$ ^{48,49}), high absorption^{48,49} and emission cross-sections^{48,49}, making it suitable for high-power ultrafast pulse generation⁴⁸⁻⁵⁰. A 5mm long Tm:Lu₂O₃ ceramic is pumped by a home-made continuous-wave Ti:sapphire laser at 796nm with 2.6W maximum power. A p -polarized pump beam is focused into the gain medium via an 80mm focal length lens and a folding mirror (with $>99\%$ transmittance at 976nm) to a spot radius of $26\mu\text{m}$ ($1/e^2$ intensity), measured in air at the location of the input facet of the ceramic. The GSA is inserted in the cavity between mirrors M1 and M2 at the Brewster's angle, to reduce Fresnel reflection loss (Fig.3). The laser beam waist radii inside the gain medium and on the GSA are calculated as $32 \times 61\mu\text{m}^2$ and $110 \times 158\mu\text{m}^2$,

respectively, by using the ray matrices method of Ref.51. A pair of infrared-grade fused silica prisms with 12cm tip-to-tip separation is used to control the intracavity net group velocity dispersion (GVD). Each prism is placed at a minimum deviation to reduce insertion losses. The total round-trip cavity GVD at $2\mu\text{m}$ is $\sim -2980\text{fs}^2$, due to the insertion of the prisms (glass material dispersion, $-113\text{fs}^2/\text{mm}$), the gain medium itself ($-15\text{fs}^2/\text{mm}$) and the angular dispersion of the prism pair (-1436fs^2). The whole cavity length is $\sim 1.35\text{m}$.

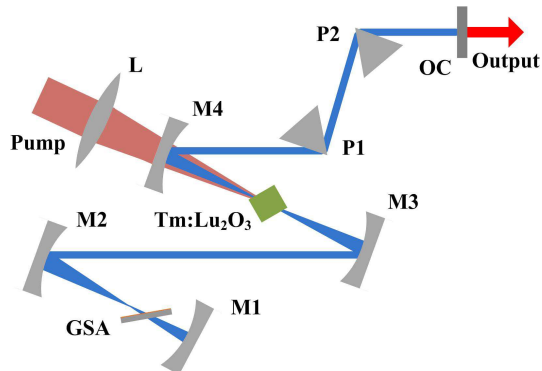


FIG. 3. Laser setup. L: lens; M1 with 75mm curvature; M2-M4 with 100mm curvature radii; P1,P2: fused silica prisms.

During continuous wave operation (without GSA) the laser produces up to 640mW output power from 1.8W of absorbed pump power at $\sim 2070\text{nm}$, the lasing threshold being 89mW. After inserting the GSA, the lasing threshold increases to 314mW. Self-starting mode-locking is achieved at 160mW average output power (with $\sim 1.16\text{W}$ absorbed pump power). The maximum average output power is 270mW, while the absorbed pump power is 1.8W. The obtained output power is comparable to that of previous $2\mu\text{m}$ SESAMs mode-locked ultrafast solid-state lasers (e.g. 155mW from $\text{Tm,Ho:NaY(WO}_4)_2$ ⁸, 325mW from $\text{Tm:Sc}_2\text{O}_3$ ⁹ lasers), but larger than thus far reported for $2\mu\text{m}$ nanotube mode-locked Tm-doped solid-state lasers (e.g. 50mW from a $\text{Tm:Lu}_2\text{O}_3$ laser⁵²) and graphene mode-locked solid-state lasers (e.g. 60mW from a Tm:CLNGG laser²⁸) in sub-ps regime. The repetition rate is $\sim 110\text{MHz}$. The corresponding pulse energy is $\sim 2.45\text{nJ}$, higher than thus far achieved for $2\mu\text{m}$ nanotube (e.g. $\sim 0.5\text{nJ}$ ⁵³)^{54,55} and graphene (e.g. $\sim 0.4\text{nJ}$ ²⁵) mode-locked fiber lasers²⁵. Higher output power/energy is possible by increasing pump power, as the output power is limited by the maximum available pump power.

The peak wavelength is 2067nm (Fig.4a). The FWHM bandwidth is $\sim 11.1\text{nm}$ at the maximum average output power. The spectrum has no soliton sidebands, unlike what typical for $2\mu\text{m}$ ultrafast fiber lasers⁵³⁻⁵⁵ due to intracavity periodical perturbations⁵⁶. Fig.4b plots the autocorrelation trace of the output pulses at the maximum average output power. The data are well fitted by a sech^2 temporal profile, giving a pulse duration $\sim 410\text{fs}$. This is longer than previously re-

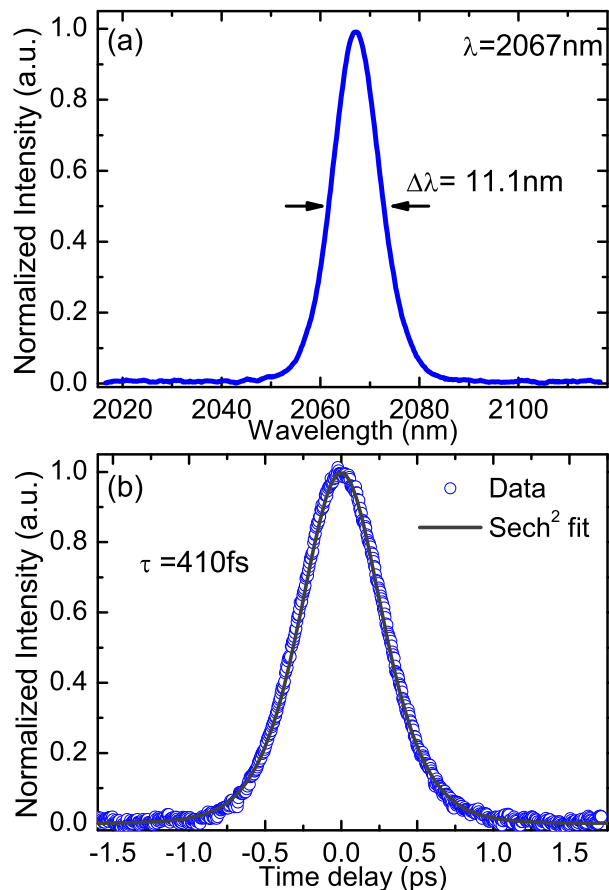


FIG. 4. (a) output spectrum, (b) autocorrelation trace.

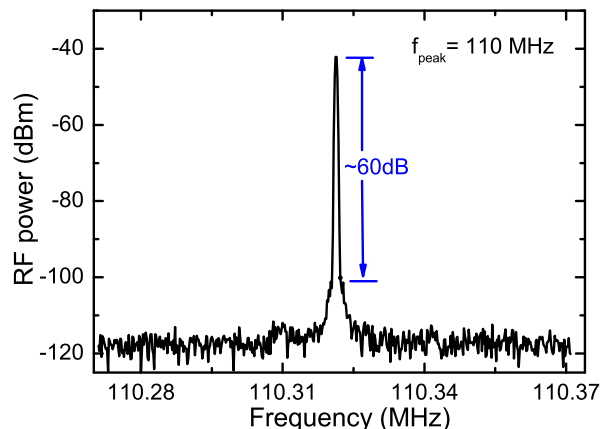


FIG. 5. RF spectrum. The resolution bandwidth is 300Hz.

ported from SESAMs and nanotube mode-locked $2\mu\text{m}$ solid-state lasers (e.g. $\sim 200\text{fs}$ ^{8,9,52}), but shorter than previous graphene mode-locked $2\mu\text{m}$ solid-state lasers (e.g. $\sim 10\text{ps}$ ²⁷, $\sim 729\text{fs}$ ²⁸). The pulse duration is much shorter than $2\mu\text{m}$ nanotube (e.g. $\sim 0.75\text{ps}$ ⁵³, $\sim 1.3\text{ps}$ ⁵⁵) and graphene (e.g. $\sim 3.6\text{ps}$ ²⁵) mode-locked fiber lasers. The time-bandwidth product is 0.319, close to 0.315 expected

for transform-limited sech^2 pulses.

The mode-locking operation stability is studied measuring the radio frequency (RF) spectrum using a fast InGaAs photo-detector ($>7\text{GHz}$ cut-off) connected to a spectrum analyzer. Fig.5 plots the RF spectrum around the fundamental repetition frequency of 110MHz. A signal-to-noise ratio of 60dB (a contrast of 10^6) is measured, implying no Q-switching instabilities⁵⁷.

In conclusion, we demonstrated a graphene mode-locked solid-state Tm:Lu₂O₃ laser at $2\mu\text{m}$, having transform-limited 410fs pulses with $\sim 270\text{mW}$ average output power, and $\sim 110\text{MHz}$ repetition rate. This showcases the potential of graphene for high-power ultrafast solid-state lasers.

We acknowledge funding from the ERC grants NANOPOTS, EU grants RODIN, MEM4WIN, GENIUS, EPSRC grants EP/GO30480/1 and EP/G042357/1, King's college Cambridge, the Royal Academy of Engineering, a Royal Society Wolfson Research Merit Award, and the Cambridge Nokia Research Centre.

- 1 V. W. S. Chan, IEEE J. Sel. Top. Quantum Elect. **6**,959 (2000)
- 2 B. E. Bouma, L. E. Nelson, G. J. Tearney, D. J. Jones, M. E. Brezinski and J. G. Fujimoto, J. Biomed. Opt. **3**,76(1998)
- 3 F. Dausinger, F. Lichtner, H. Lubatschowski, Femtosecond Technology for Technical and Medical Applications, Springer, 2004
- 4 R. R. Gattass, E. Mazur, Nat. Phot. **2**,219 (2008)
- 5 M. Ebrahim-Zadeh, I. T. Sorokina, Mid-infrared Coherent Sources And Applications, Springer, 2008
- 6 U. Keller, Nature **424**,831(2003)
- 7 W. Sibbett, A. A. Lagatsky, C. T. A. Brown, Opt. Expr. **20**,6989 (2012)
- 8 A. A. Lagatsky, X. Han, M. D. Serrano, C. Cascales, C. Zaldo, S. Calvez, M. D. Dawson, J. A. Gupta, C. T. A. Brown, W. Sibbett, Opt. Lett. **35**, 3027 (2010)
- 9 A. A. Lagatsky, P. Koopmann, P. Fuhrberg, G. Huber, C. T. A. Brown, W. Sibbett, Opt. Lett. **37**, 437 (2012)
- 10 T. Hasan, Z. Sun, F. Wang, F. Bonaccorso, P. H. Tan, A. G. Rozhin, A. C. Ferrari, Adv. Mater. **21**, 3874 (2009)
- 11 Z. Sun, T. Hasan, A. C. Ferrari, Physica E **44**, 921 (2012)
- 12 F. Bonaccorso, Z. Sun, T. Hasan, A. C. Ferrari, Nat. Phot **4**,611(2010)
- 13 D. Popa, Z. Sun, T. Hasan, W. B. Cho, F. Wang, F. Torrisi, A. C. Ferrari, Appl. Phys. Lett. **101**, 153107 (2012)
- 14 Z. Sun, T. Hasan, F. Torrisi, D. Popa, F. Bonaccorso, D. M. Basko, A. C. Ferrari, ACS Nano **4**, 803 (2010)
- 15 F. Torrisi, T. Hasan, W. Wu, S. Jung, F. Bonaccorso, P. J. Paul, D. P. Chu, A. C. Ferrari, ACS Nano **6**, 2992 (2012).
- 16 F. Wang, A. G. Rozhin, V. Scardaci, Z. Sun, F. Henrich, I. H. White, W. I. Milne, A. C. Ferrari, Nat. Nano. **3**, 738 (2008)
- 17 I. H. Baek, H. W. Lee, S. Bae, B. H. Hong, Y. H. Ahn, D. I. Yeom, F. Rotermund, Appl. Phys. Express **5**, 032701 (2012)
- 18 W. D. Tan, C. Y. Su, R. J. Knize, G. Q. Xie, L. J. Li, D. Y. Tang, Appl. Phys. Lett. **96**, 031106 (2010)
- 19 W. B. Cho, J. H. Yim, S. Y. Choi, S. Lee, U. Griebner, V. Petrov, F. Rotermund, Opt. Lett. **33**, 2449 (2008)
- 20 Z. Sun, D. Popa, T. Hasan, F. Torrisi, F. Wang, E. Kelleher, V. Nicolosi, A. Ferrari, Nano Res. **3**, 653 (2010)
- 21 Q. Bao, H. Zhang, Y. Wang, Z. Ni, Y. Yan, Z. X. Shen, K. P. Loh, and D. Y. Tang, Adv. Funct. Mater. **19**, 3077 (2009)
- 22 T. Hasan, F. Torrisi, Z. Sun, D. Popa, V. Nicolosi, A. C. Ferrari, Phys. Stat. Sol. (b) **247**, 2953 (2010)
- 23 D. Popa, Z. Sun, F. Torrisi, T. Hasan, F. Wang, A. C. Ferrari, Appl. Phys. Lett. **97**, 203106 (2010)
- 24 Y. Hernandez, V. Nicolosi, M. Lotya, F. M. Blighe, Z. Y. Sun, S. De, I. T. McGovern, B. Holland, M. Byrne, Y. K. Gunko, J. J. Boland, P. Niraj, G. Duesberg, S. Krishnamurthy, R. Goodhue, J. Hutchison, V. Scardaci, A. C. Ferrari, J. N. Coleman, Nat. Nano. **3**, 563 (2008)
- 25 M. Zhang, E. J. R. Kelleher, F. Torrisi, Z. Sun, T. Hasan, D. Popa, F. Wang, A. C. Ferrari, S. V. Popov, J. R. Taylor, Optics Express **20**, 25077 (2012)
- 26 L. E. Nelson, D. J. Jones, K. Tamura, H. A. Haus, and E. P. Ippen, Appl. Phys. B **65**, 277 (1997)
- 27 J. Liu, Y. G. Wang, Z. S. Qu, L. H. Zheng, L. B. Su and J. Xu, Laser Phys. Lett. **9**, 15 (2012)
- 28 J. Ma, G. Q. Xie, P. Lv, W. L. Gao, P. Yuan, L. J. Qian, H. H. Yu, H. J. Zhang, J. Y. Wang, D. Y. Tang, Opt. Lett. **37**, 2085 (2012)
- 29 S. Stankovich, D. A. Dikin, G. H. B. Dommett, K. M. Kohlhaas, E. J. Zimney, E. A. Stach, R. D. Piner, S. T. Nguyen, R. S. Ruoff, Nature **442**, 282 (2006)
- 30 C. Mattevi, G. Eda, S. Agnoli, S. Miller, K. A. Mkhoyan, O. Celik, D. Mestrogiovanni, G. Granozzi, E. Garfunkel, M. Chhowalla, Adv. Funct. Mater. **19**, 2577 (2009)
- 31 S. Bae, H. Kim, Y. Lee, X. Xu, J. S. Park, Y. Zheng, J. Balakrishnan, T. Lei, H. R. Kim, Y. I. Song, Y. J. Kim, K. S. Kim, B. Ozyilmaz, J. H. Ahn, B. H. Hong, S. Iijima, Nat. Nano. **5**, 574 (2010)
- 32 X. Li, W. Cai, J. An, S. Kim, J. Nah, D. Yang, R. Piner, A. Velamakanni, I. Jung, E. Tutuc, S. K. Banerjee, L. Colombo, R. S. Ruoff, Science **324**, 1312 (2009)
- 33 A. C. Ferrari, J. C. Meyer, V. Scardaci, C. Casiraghi, M. Lazzeri, F. Mauri, S. Piscanec, D. Jiang, K. S. Novoselov, S. Roth, and A. K. Geim, Phys. Rev. Lett. **97**, 187401 (2006).
- 34 L. G. Cancado, A. Jorio, E. H. M. Ferreira, F. Stavale, C. A. Achete, R. B. Capaz, M. V. O. Moutinho, A. Lombardo, T. S. Kulmala, A. C. Ferrari, Nano Lett. **11**, 3190 (2011)
- 35 A. Mooradian, Phys. Rev. Lett. **22**, 185 (1969).
- 36 A. C. Ferrari, J. Robertson, Phys. Rev. B **61**, 14095 (2000)
- 37 A. Pirkle, J. Chan, A. Venugopal, D. Hinojos, C. W. Magnuson, S. McDonnell, L. Colombo, E. M. Vogel, R. S. Ruoff, R. M. Wallace, Appl. Phys. Lett. **99**, 122108 (2011)
- 38 A. Ferrari, Solid State Comm. **143**, 47 (2007)
- 39 A. Das, S. Pisana, B. Chakraborty, S. Piscanec, S. K. Saha, U. V. Waghmare, K. S. Novoselov, H. R. Krishnamurthy, A. K. Geim, A. C. Ferrari, A. K. Sood, Nat. Nano. **3**, 210 (2008)
- 40 C. Casiraghi, S. Pisana, K. S. Novoselov, A. K. Geim, A. C. Ferrari, Appl. Phys. Lett. **91**, 233108 (2007)
- 41 S. Pisana, M. Lazzeri, C. Casiraghi, K. S. Novoselov, A. K. Geim, A. C. Ferrari, F. Mauri, Nat. Mater. **6**, 198 (2007)
- 42 Y. Y. Wang, Z. H. Ni, T. Yu, Z. X. Shen, Y. H. Wu, W. Chen, and A. T. Shen Wee, J. Phys. Chem. C **112**, 10637 (2008)
- 43 L. Kong, J. Phys. Chem. C **114**, 21618 (2010)
- 44 V. G. Kravets, A. N. Grigorenko, R. R. Nair, P. Blake, S. Anissimova, K. S. Novoselov, A. K. Geim, Phys. Rev. B **81**, 155413 (2010)
- 45 G. P. Agrawal, *Applications of Nonlinear Fiber Optics*. (Academic Press, London, 2001).
- 46 R. R. Nair, P. Blake, K. S. Novoselov, T. J. Booth, T. Stauber, N. M. R. Peres, A. K. Geim, Science **320**, 1308 (2008)
- 47 K. F. Mak, M. Y. Sfeir, Y. Wu, C. H. Lui, J. A. Misewich, and T. F. Heinz, Phys. Rev. Lett. **101**, 196405 (2008).
- 48 P. Koopmann, R. Peters, K. Petermann and G. Huber, Appl. Phys. B **102**, 19 (2011)
- 49 L. A. Oleg, S. Y. Golovkin, O. N. Gorshkov, N. G. Zakharov, M. V. Kruglova, M. O. Marychev, A. A. Novikov, N. V. Sakharov, E. V. Chuprunov, Quantum Electron. **41**, 863 (2011)
- 50 A. A. Lagatsky, O. L. Antipov, W. Sibbett, Opt. Expr. **20**, 19349 (2012)
- 51 W. Koechner, Solid-State Laser Engineering., Springer, 2006
- 52 A. Schmidt, P. Koopmann, G. Huber, P. Fuhrberg, S. Y. Choi, F. Rotermund, V. Petrov, U. Griebner, Opt. Expr. **20**, 5313 (2012)
- 53 K. Kieu, F. W. Wise, IEEE Phot. Tech. Lett. **21**, 128 (2009)
- 54 S. Kivisto, T. Hakulinen, A. Kaskela, B. Aitchison, D. P. Brown, A. G. Nasibulin, E. I. Kauppinen, O. G. Okhotnikov, Opt. Expr. **17**, 2358 (2009)
- 55 M. A. Solodyankin, E. D. Obraztsova, A. S. Lobach, A. I. Chernov, V. I. Konov, E. M. Dianov, Opt. Lett. **33**, 1336 (2008)
- 56 M. L. Dennis, I. N. Duling, IEEE J. Quan. Electr. **30**, 1469 (1994)
- 57 C. Honninger, R. Paschotta, F. Morier-Genoud, M. Moser, U. Keller, J. Opt. Soc. Am. B **16**, 46 (1999)